

Light dilaton in a metastable vacuumDaniel Elander¹, Maurizio Piai,² and John Roughley²¹*Laboratoire Charles Coulomb (L2C), University of Montpellier, CNRS, 34095 Montpellier, France*²*Department of Physics, College of Science, Swansea University, Singleton Park, SA2 8PP Swansea, Wales, United Kingdom*

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We identify a parametrically light dilaton by studying the perturbations of metastable vacua along a branch of regular supergravity backgrounds that are dual to four-dimensional confining field theories. The branch includes also stable and unstable solutions. The former encompass, as a special case, the geometry proposed by Witten as a holographic model of confinement. The latter approach a supersymmetric solution, by enhancing a condensate in the dual field theory. A phase transition separates the space of stable backgrounds from the metastable ones. In proximity of the phase transition, one of the lightest scalar states inherits some of the properties of the dilaton, despite not being particularly light.

DOI: [10.1103/PhysRevD.103.046009](https://doi.org/10.1103/PhysRevD.103.046009)**I. INTRODUCTION**

The Higgs particle [1,2] might originate as a composite dilaton in a new strongly coupled theory. The literature on the effective field theory description of the dilaton has an ancient origin [3,4]. It has been invoked in the context of dynamical electroweak symmetry breaking [5–7], of extensions of the standard model [8–19], and in the interpretation of lattice data [20–30]. With the advent of gauge-gravity dualities [31–34], holographic models giving rise to a dilatonic state have been identified and studied both in the context of bottom-up [35–49] and top-down constructions derived from supergravity [50–54].

We pursue an alternative approach to the study of the dilaton, along the program announced in Ref. [55], which is inspired by Refs. [56–59], but is implemented within the rigorous framework of supergravity. We generalize the notion of proximity to the Breitenlohner-Freedman unitarity bound [60]—central to the arguments in Ref. [56]—in order to explore non-AdS (anti-de Sitter) backgrounds dual to confining theories, in regions of parameter space near tachyonic instabilities. We aim at ascertaining whether the spectrum of bound states includes a light dilaton.

In this paper we consider the toroidal compactification of the maximal supergravity theory in $D = 7$ dimensions [61–65], that admits as a background solution the holographic description of confinement proposed by Witten

[66]—also used for phenomenological purposes by Sakai and Sugimoto [67,68]. We compare to the case of Romans theory [69]—see Refs. [55,70,71].

We focus on three branches of solutions: (i) regular solutions that include the Witten model and are interpreted as duals of four-dimensional confining theories, (ii) a class of supersymmetric solutions, and (iii) a branch of nonsupersymmetric solutions, that (locally) preserve six-dimensional Poincaré invariance but are badly singular—they do not even meet Gubser’s criteria [72]. We compute the spectrum of fluctuations of the relevant scalar and spin-2 tensor states, using the gauge-invariant formalism of Refs. [73–77], hence extending the study of the spectra performed in Refs. [70,78]. We compare to the result of applying the probe approximation [79] in order to ascertain whether any of the scalar states have significant overlap with the trace of the stress-energy tensor and can hence be identified with an approximate dilaton.

In a region of parameter space the spectrum contains a parametrically light dilaton. We study the energetics along the three branches of solutions, by computing the free energy using holographic renormalization [80–82], and employing a simple scale-setting procedure to compare different backgrounds [83]. We present firm evidence of the existence of a phase transition in the gravity theory (see also Ref. [84]). The parametrically light dilaton emerges along the portion of the regular branch of solutions which contains metastable solutions, the lifetime of which is not known (but see Ref. [85]).

II. THE GRAVITY MODEL

We denote with hatted symbols quantities characterizing the theory in $D = 7$ dimensions. The action, truncated to

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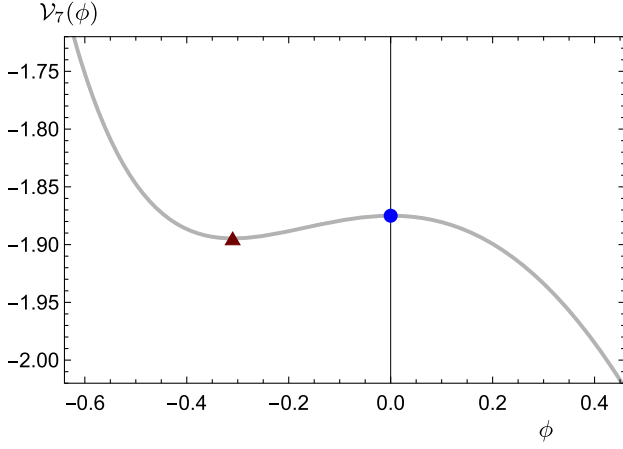


FIG. 1. The potential $\mathcal{V}_7(\phi)$ of the theory. The blue disk is the ϕ_{UV} critical point, while the red triangle is the ϕ_{IR} one.

retain the scalar ϕ coupled to gravity, is the following [79] (see also Refs. [62,63,70]):

$$\mathcal{S}_7 = \int d^7x \sqrt{-\hat{g}_7} \left[\frac{\mathcal{R}_7}{4} - \frac{\hat{g}^{\hat{M}\hat{N}}}{4} \partial_{\hat{M}} \phi \partial_{\hat{N}} \phi - \mathcal{V}_7 \right], \quad (1)$$

where the potential (see Fig. 1) is

$$\mathcal{V}_7 = \frac{1}{8} e^{-\frac{8}{\sqrt{5}}\phi} - e^{-\frac{3}{\sqrt{5}}\phi} - e^{\frac{2}{\sqrt{5}}\phi}. \quad (2)$$

This potential admits two critical points. The one with $\phi = \phi_{\text{UV}} = 0$ will play a central role in this paper, as it corresponds to a UV fixed point in the dual field theory. It yields $\mathcal{V}_7(\phi_{\text{UV}}) = -\frac{15}{8}$. Another critical point of \mathcal{V}_7 has $\phi_{\text{IR}} = -\frac{1}{\sqrt{5}} \log(2)$, for which $\mathcal{V}_7(\phi_{\text{IR}}) = -\frac{5}{2^{7/5}}$.

Following the notation in Refs. [70,79], we reduce to $D = 5$ dimensions by adopting the following ansatz:

$$ds_7^2 = e^{-2\chi} ds_5^2 + e^{3\chi-2\omega} d\eta^2 + e^{3\chi+2\omega} d\zeta^2, \quad (3)$$

where the metric ds_5^2 takes the domain wall form

$$ds_5^2 = e^{2A(r)} dx_{1,3}^2 + dr^2, \quad (4)$$

and the background profiles $\phi(r)$, $\chi(r)$, $\omega(r)$, and $A(r)$ depend only on the radial coordinate r . The angles $0 \leq \eta, \zeta < 2\pi$ parametrize a torus. We apply the change of variables $d\rho = e^{-\chi} dr$. The domain-wall (DW) ansatz in $D = 7$ dimensions is recovered by imposing the constraints $\omega = 0$ and $\mathcal{A} = A - \chi = \frac{3}{5}A = \frac{3}{5}\chi$, and hence the AdS₇ solution has $\partial_\rho \mathcal{A} = \frac{1}{2}$, $\partial_\rho \chi = \frac{1}{3}$, and $\partial_\rho A = \frac{5}{6}$. The bulk action in $D = 5$ dimensions is the following:

$$\mathcal{S}_5 = \int d^5x \sqrt{-g_5} \left[\frac{\mathcal{R}_5}{4} - \frac{g^{MN}}{2} G_{ab} \partial_M \Phi^a \partial_N \Phi^b - \mathcal{V} \right], \quad (5)$$

where $\mathcal{V} = e^{-2\chi} \mathcal{V}_7$, $\Phi^a = \{\phi, \omega, \chi\}$, and the sigma-model metric is $G_{ab} = \text{diag}(\frac{1}{2}, 1, \frac{15}{4})$. We verified that

$$\mathcal{S}_7 = \int d\eta d\zeta \left[\mathcal{S}_5 + \int d^5x \partial_M \left(\frac{1}{2} \sqrt{-g_5} g^{MN} \partial_N \chi \right) \right]. \quad (6)$$

III. CLASSES OF SOLUTIONS

All the solutions of interest approach $\phi = \phi_{\text{UV}} = 0$ at large ρ . We write them as a power series of the small coordinate $z \equiv e^{-\rho/2}$, as follows

$$\begin{aligned} \phi(z) &= \phi_2 z^2 + \left(\phi_4 - \frac{18\phi_2^2 \log(z)}{\sqrt{5}} \right) z^4 \\ &+ \left(\frac{162}{5} \phi_2^3 \log(z) - \frac{637\phi_2^3}{30} - \frac{9\phi_2\phi_4}{\sqrt{5}} \right) z^6 + \dots, \end{aligned} \quad (7)$$

$$\omega(z) = \omega_U + \omega_6 z^6 + \dots, \quad (8)$$

$$\begin{aligned} \chi(z) &= \chi_U - \frac{2}{3} \log(z) - \frac{\phi_2^2 z^4}{30} + \frac{2}{675} \left(\frac{675}{2} \chi_6 - 150\omega_6 \right. \\ &\left. + 72\sqrt{5}\phi_2^3 \log(z) - 6\sqrt{5}\phi_2^3 - 20\phi_2\phi_4 \right) z^6 + \dots, \end{aligned} \quad (9)$$

$$\begin{aligned} A(z) &= A_U - \frac{5}{3} \log(z) - \frac{\phi_2^2 z^4}{12} + \frac{1}{270} \left(\frac{135}{2} \chi_6 - 30\omega_6 \right. \\ &\left. + 144\sqrt{5}\phi_2^3 \log(z) - 12\sqrt{5}\phi_2^3 - 40\phi_2\phi_4 \right) z^6 + \dots. \end{aligned} \quad (10)$$

They are characterized by seven integration constants: ϕ_2 , ϕ_4 , ω_U , ω_6 , χ_U , χ_6 , and A_U . The DW solutions have $\omega_U = \omega_6 = \chi_6 = 0$ and $\chi_U = \frac{2}{5}A_U$, leaving A_U , ϕ_2 and ϕ_4 as independent nontrivial free parameters. What we will call confining solutions have $\chi_6 = 0$.

We find it convenient to define a scale Λ as follows [83]:

$$\Lambda^{-1} \equiv \int_{\rho_o}^{\infty} d\rho e^{\chi(\rho) - A(\rho)}, \quad (11)$$

with ρ_o as the end of space. While other choices might be admissible, this has the advantage of being applicable to all the solutions of interest.

A. SUSY solutions

The supersymmetric (SUSY) DW solutions satisfy the following first-order differential equations:

$$\partial_\rho \mathcal{A} = -\frac{2}{5} \mathcal{W}_1, \quad \partial_\rho \phi = 2\partial_\phi \mathcal{W}_1. \quad (12)$$

The superpotential $\mathcal{W}_1 \equiv -\frac{1}{4} e^{-\frac{4}{\sqrt{5}}\phi} - e^{\frac{1}{\sqrt{5}}\phi}$ solves the defining equation $\mathcal{V}_D = \frac{1}{2} G^{\phi\phi} (\partial_\phi \mathcal{W})^2 - \frac{D-1}{D-2} \mathcal{W}^2$ for $D = 7$.

After performing the change of variables $\partial_\rho \equiv e^{-\frac{3\phi}{2\sqrt{5}}}\partial_\tau$, we find the exact solutions

$$\phi(\tau) = \frac{4}{\sqrt{5}} \operatorname{arctanh}(e^{-2(\tau-\tau_o)}), \quad (13)$$

with the warp factor given by

$$\mathcal{A}(\tau) = \mathcal{A}_o + \frac{1}{10} \log[\cosh(\tau - \tau_o) \sinh^4(\tau - \tau_o)], \quad (14)$$

where \mathcal{A}_o and τ_o are real integration constants.

The IR expansion of these solutions in terms of the radial coordinate ρ and the new constants ρ_o and $\mathcal{A}_I = \mathcal{A}_0 + \log(\frac{\rho}{5})$ can be written explicitly in the following form

$$\phi(\rho) = -\sqrt{5} \log \frac{2(\rho - \rho_o)}{5} + \frac{16(\rho - \rho_o)^5}{1875\sqrt{5}} + \dots, \quad (15)$$

and

$$\mathcal{A}(\rho) = \mathcal{A}_I + \log(\rho - \rho_o) + \frac{8(\rho - \rho_o)^5}{9375} + \dots \quad (16)$$

Their holographic interpretation involves an operator of dimension $\Delta = 4$ developing a vacuum expectation value in the dual field theory.

The conjugate superpotential entering the calculation of the free energy is known as a perturbative expansion:

$$\mathcal{W}_2 = -\frac{5}{4} - \frac{\phi^2}{4} + \frac{3\phi^3}{4\sqrt{5}} \log\left(\frac{\phi^2}{\kappa}\right) + \dots, \quad (17)$$

where κ is scheme dependent.

B. Singular DW solutions

A class of singular DW solutions is characterized by the harmless \mathcal{A}_I , the end of space ρ_o , and the nontrivial ϕ_5 . As anticipated, these solutions are badly singular: their Ricci scalar tensor \mathcal{R}_7 diverges, and the potential is not bounded from above, violating the requirement from Ref. [72]. The IR expansion of solutions of this class reads as follows:

$$\begin{aligned} \phi(\rho) &= \frac{\sqrt{5}}{4} \log \frac{8}{5} (\rho - \rho_o) + \phi_5 (\rho - \rho_o)^{5/8} \\ &+ \frac{1}{135} (37\sqrt{5}\phi_5^2 - 242^{3/4}\sqrt{5}) (\rho - \rho_o)^{5/4} + \dots, \end{aligned} \quad (18)$$

$$\begin{aligned} \mathcal{A}(\rho) &= \mathcal{A}_I + \frac{\log(\rho - \rho_o)}{16} + \frac{4\phi_5}{3\sqrt{5}} (\rho - \rho_o)^{5/8} \\ &+ \frac{1}{2700} (192 \times 10^{3/4} - 2155\phi_5^2) (\rho - \rho_o)^{5/4} + \dots \end{aligned} \quad (19)$$

C. Confining solutions

The regular solutions of this class obey the constraint $A = \frac{5}{2}\chi + \omega$. They depend on two harmless constants χ_I and ω_I , besides ρ_o and ϕ_I . The IR expansion of these solutions reads as follows:

$$\begin{aligned} \phi(\rho) &= \phi_I - \frac{1}{2\sqrt{5}} (\rho - \rho_o)^2 e^{-\frac{8\phi_I}{\sqrt{5}}} (-3e^{\sqrt{5}\phi_I} + 2e^{2\sqrt{5}\phi_I} + 1) \\ &+ \dots, \end{aligned} \quad (20)$$

$$\begin{aligned} \omega(\rho) &= \omega_I - \frac{\log(\rho - \rho_o)}{2} \\ &+ \frac{1}{40} (\rho - \rho_o)^2 e^{-\frac{8\phi_I}{\sqrt{5}}} (8e^{\sqrt{5}\phi_I} + 8e^{2\sqrt{5}\phi_I} - 1) + \dots, \end{aligned} \quad (21)$$

$$\begin{aligned} \chi(\rho) &= \chi_I + \frac{\log(\rho - \rho_o)}{3} \\ &+ \frac{1}{6000} (\rho - \rho_o)^4 e^{-\frac{16\phi_I}{\sqrt{5}}} (32e^{\sqrt{5}\phi_I} - 56e^{2\sqrt{5}\phi_I} \\ &+ 224e^{3\sqrt{5}\phi_I} + 32e^{4\sqrt{5}\phi_I} - 7) + \dots \end{aligned} \quad (22)$$

We restrict attention to solutions flowing from the UV critical point, which requires $\phi_I > \phi_{\text{IR}}$. The invariants \mathcal{R}_7 , $\mathcal{R}_{7\hat{M}\hat{N}}\mathcal{R}_7^{\hat{M}\hat{N}}$, and $\mathcal{R}_7^{\hat{P}}{}_{\hat{M}\hat{N}\hat{Q}}\mathcal{R}_7^{\hat{M}\hat{N}\hat{Q}}$ are finite. We impose the constraint $\omega_I = \frac{3}{2}\chi_I$ in order to avoid a conical singularity.

IV. GLUEBALL MASSES

We compute the spectrum of fluctuations of the five-dimensional theory, by employing the gauge-invariant formalism developed in Refs. [73–77]. We introduce the IR regulator ρ_1 with $\rho_o < \rho_1$, and the UV regulator ρ_2 . The physical results are recovered in the limits $\rho_1 \rightarrow \rho_o$ and $\rho_2 \rightarrow +\infty$ (see Refs. [70,71,77]). The scalar fluctuations are written as the gauge invariant combinations

$$\mathbf{a}^a(M, \rho) \equiv \varphi^a(M, \rho) - \frac{\partial_\rho \Phi^a(\rho)}{6\partial_\rho A(\rho)} h(M, \rho), \quad (23)$$

where M is the mass in the dual theory, φ^a are fluctuations of the scalars Φ^a and h of the trace of the four-dimensional portion of the metric. They obey the following linearized equations and boundary conditions:

$$0 = [e^\chi \partial_\rho (e^{-\chi} \partial_\rho) + (4\partial_\rho A) \partial_\rho + e^{2\chi-2A} M^2] \mathbf{a}^a - e^{2\chi} \chi^a{}_c \mathbf{a}^c, \quad (24)$$

$$\begin{aligned} 0 &= e^{-2\chi} \partial_\rho \Phi^c \partial_\rho \Phi^d G_{db} \partial_\rho \mathbf{a}^b + \left[\frac{3\partial_\rho A}{2} e^{-2A} M^2 \delta^c{}_b \right. \\ &\left. - \partial_\rho \Phi^c \left(\frac{4\mathcal{V}}{3\partial_\rho A} \partial_\rho \Phi^d G_{db} + \frac{\partial \mathcal{V}}{\partial \Phi^b} \right) \right] \mathbf{a}^b \Big|_{\rho_i}, \end{aligned} \quad (25)$$

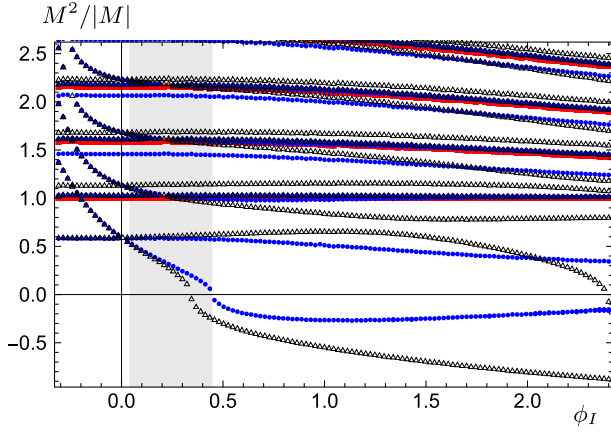


FIG. 2. The spectra of scalar masses M as a function of the parameter ϕ_I along the confining branch of solutions, normalized in units of the lightest tensor mass, and using regulators $\rho_1 = 10^{-4}$ and $\rho_2 = 12$. The (red) squares represent the spin-2 tensor modes, the (blue) disks are the scalar, gauge invariant fluctuations originating from ϕ , χ , and ω . The (black) triangles do not represent an additional set of states: they denote the same scalars, but computed in the probe approximation—neglecting the fluctuation of the background metric. The shading denotes the stable (leftmost white), metastable (gray), and unstable (rightmost white) backgrounds. We verified that our choices for the two regulators were sufficiently close to the physical limits ($\rho_1 \rightarrow \rho_o$, $\rho_2 \rightarrow \infty$) to avoid discernible cutoff effects.

where in all these expressions the quantities A , Φ^a , and \mathcal{V} are evaluated on the background, and

$$\begin{aligned} \chi^a{}_c \equiv & \partial_c \left[G^{ab} \frac{\partial \mathcal{V}}{\partial \Phi^b} \right] \\ & + \frac{4}{3\partial_\rho A} \left[\partial_\rho \Phi^a \frac{\partial \mathcal{V}}{\partial \Phi^c} + G^{ab} \frac{\partial \mathcal{V}}{\partial \Phi^b} \partial_\rho \Phi^d G_{dc} \right] \\ & + \frac{16\mathcal{V}}{9(\partial_\rho A)^2} \partial_\rho \Phi^a \partial_\rho \Phi^b G_{bc}. \end{aligned} \quad (26)$$

The gauge invariant spin-2 tensor fluctuations obey the linearized equation

$$0 = [\partial_\rho^2 + (4\partial_\rho A - \partial_\rho \chi)\partial_\rho + e^{2\chi-2A}M^2]e^\mu{}_\nu, \quad (27)$$

and Neumann boundary conditions $\partial_\rho e^\mu{}_\nu|_{\rho_i} = 0$.

The probe approximation for the scalars is defined by ignoring the term proportional to h in Eq. (24). According to the dictionary of gauge-gravity dualities, h is the bulk field associated with the trace of the stress-energy tensor, which is the field theory operator associated with dilatation, and sourcing the dilaton. Hence, this approximation holds for scalar bound states that decouple from the dilatation operator, and cannot be interpreted as a dilaton. The equations for the scalar fluctuations greatly simplify, as only the first term in Eq. (26) survives, and the boundary conditions reduce to Dirichlet. Note that the probe

approximation is used solely as a diagnostic tool to identify scalar states which mix nontrivially with the dilaton.

In Fig. 2, we show the spectra of tensors and scalars, compared to the probe approximation, normalized to the lightest spin-2 fluctuation. For $\phi_I < 0$ the scalars agree with Ref. [70]. The new results for $\phi_I > 0$ show that one of the scalars becomes parametrically light, and eventually tachyonic, for positive ϕ_I . The mass vanishes exactly at some finite value of ϕ_I , for which the background geometry is still describing the dual of a confining field theory, in the presence of nonvanishing condensates. When this state is light, or tachyonic, the probe approximation does not capture it correctly, indicating that the state has a nontrivial component along h , and hence is sourced by the trace of the stress-energy tensor, as expected by a dilaton. We also notice that several of the heavy scalar states are not well captured by the probe approximation, showing that mixing effects with the dilaton are not restricted to the lightest states.

V. FREE ENERGY

To compute the free energy, we write explicitly the boundary terms of the theory in $D = 7$ dimensions:

$$S = S_7 + \sum_{i=1,2} (-)^i \int d^4x d\zeta d\eta \sqrt{-\tilde{g}} \left[\frac{K}{2} + \lambda_i \right]_{\rho=\rho_i}, \quad (28)$$

where \tilde{g} denotes the determinant of the pullback of the induced metric, K is the Gibbons-Hawking-York term and λ_i are localized boundary potentials.

The potential terms are chosen according to the same prescription as in Ref. [55]: in the UV we replace $\lambda_2 = \mathcal{W}_2$, which allows one to cancel all the divergences and perform the program of holographic renormalization [80–82], while in the IR we impose $\lambda_1 = -\frac{3}{2}\partial_\rho A(\rho)$, in such a way that the variational problem be well defined in the presence of the IR boundary at $\rho = \rho_1$. The free energy density \mathcal{F} is defined in terms of the complete on-shell action to be

$$\int d^4x d\zeta d\eta \mathcal{F} \equiv - \lim_{\rho_2 \rightarrow \infty} \lim_{\rho_1 \rightarrow \rho_o} S_{\text{on-shell}}. \quad (29)$$

By making use of the equations of motion we arrive at

$$\mathcal{F} = - \lim_{\rho_2 \rightarrow \infty} e^{4A-\chi} \left(\frac{3}{2} \partial_\rho A + \mathcal{W}_2 \right) \Big|_{\rho_2}, \quad (30)$$

which is identical to Eq. (5.22) of Ref. [55].

We make use of the UV expansions of the background solutions of interest. By replacing the UV expansions in Eqs. (7)–(10) into the form of the free energy density in Eq. (30), supplemented by the specific form of the superpotential \mathcal{W}_2 in Eq. (17), we arrive at the expression:

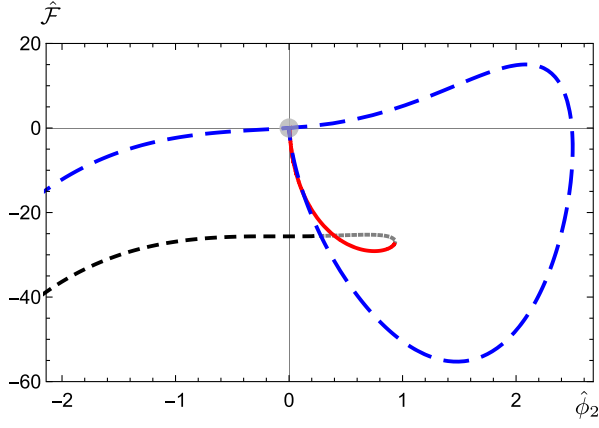


FIG. 3. The free energy density $\hat{\mathcal{F}} = \mathcal{F}\Lambda^{-6}$ as a function of the deformation parameter $\hat{\phi}_2 = \phi_2\Lambda^{-2}$. The black (dashed), gray (short dashed), and red (solid) lines represent the stable, meta-stable and unstable portions of the confining branch of solutions. In blue (long dashed) we show the singular DW solutions. The SUSY solutions are represented by the gray disk at the origin of the plot.

$$\mathcal{F} = -\frac{e^{4A_U - \chi_U}}{120} \left(20\phi_2\phi_4 - 135\chi_6 + 60\omega_6 + 12\sqrt{5}\phi_2^3 \left(-2 + \frac{3}{2} \log\left(\frac{\phi_2^2}{\kappa}\right) \right) \right). \quad (31)$$

The divergence of the contribution to the free energy proportional to ϕ_2^2 is canceled by \mathcal{W}_2 . This implies that, as for the circle reduction of the Romans supergravity [55], the concavity theorems do not apply to \mathcal{F} . This expression still contains a residual scheme dependence in the logarithmic term. We set $\kappa = e^{-4/3}$, and hence our final expression for the free energy density is

$$\mathcal{F} = -\frac{e^{4A_U - \chi_U}}{120} (20\phi_2\phi_4 - 135\chi_6 + 60\omega_6 + 18\sqrt{5}\phi_2^3 \log(\phi_2^2)). \quad (32)$$

We also remind the reader that $\chi_6 = 0$ in the background solutions of interest.

In Fig. 3 we show the free energy of the three classes of solutions, as a function of the deforming parameter $\hat{\phi}_2 \equiv \phi_2\Lambda^{-2}$, and setting $A_U = 0 = \chi_U$. The parameters ϕ_4 and ω_6 are response functions, themselves determined nonlinearly, on each branch of solutions, by the choice of ϕ_2 . The SUSY solutions have $\mathcal{F} = 0$.

The figure shows evidence of the existence of a first-order phase transition. The confining solutions minimize $\hat{\mathcal{F}}$

for negative ϕ_I . For $\phi_I > \phi_I^c$, with $\phi_I^c \simeq 0.039$ the critical value (corresponding to $\hat{\phi}_2^c \simeq 0.281$), the singular DW solutions have lower, finite free energy density $\hat{\mathcal{F}}$, so that the solutions along the confining branch are at best metastable when $\phi_I > \phi_I^c$, and eventually become unstable, with one of their fluctuations becoming tachyonic when $\phi_I \gtrsim 0.447$. Most interestingly, along the metastable branch, the lightest state becomes parametrically light, before becoming tachyonic (see Fig. 2). The probe approximation fails to capture correctly its mass squared when it is either small or negative. This eigenstate of the system is hence an admixture containing a significant contribution from the trace of the fluctuation of the metric—we interpret this finding as evidence that the state is approximately a dilaton.

VI. OUTLOOK

We presented evidence of the emergence of a parametrically light dilaton state along the metastable portion of a branch of regular backgrounds of the supergravity system in $D = 7$ dimensions that yields also the Witten model, the first known holographic description of a four-dimensional confining theory [66]. Furthermore, the results of our analysis confirm, in the rigorous context of top-down holography, the expectations from Ref. [59] that along the stable portion of the regular branch a dilaton state persists, but it is not parametrically light.

The metastable vacua, and the accompanying parametrically light dilaton state, are new findings. Comparison with Ref. [55] indicates that this is a generic feature, which emerges in a broad class of theories. It would be interesting to discover examples in which the phase transition is weaker, and the spectrum along the stable branch exhibits a light approximate dilaton. It would also be useful to identify the requirements a supergravity theory must fulfil for such features to emerge.

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Correction: Minor errors were found in Eq. (32) and the inline equation appearing before it and have been fixed. The fifth sentence that previously appeared after Eq. (32) has been deleted. The terms ϕ_5^c and $\hat{\mathcal{F}}$ have been deleted from the first parenthetical phrase appearing in the last paragraph of Sec. V. Figure 3 contained an error and has been replaced.